1. TODAY'S TWISTER

NAME

Put the numbers 1 - 8 into the boxes so that each number is used once and there are no adjoining boxes with consecutive numbers. (They may not even join at corners.)

3.

TODAY'S TWISTER

NAME $\qquad$

Name the two numbers
which have a sum of 221 and a difference of 39.
2. TODAY'S TWISTER

NAME $\qquad$

What number has its half, its double, and its third add up to 68?

ANSWER

## 4. <br> TODAY'S TWISTER

NAME $\qquad$

Can you arrange the nine sticks in such a way as to have three rectangles with equal dimensions? You may move only two sticks. Practice on another paper.


## TODAY'S TWISTER

5. NAME $\qquad$

There is a queen just below a queen.
There is a jack just above a queen.
There is a spade just above a spade.
There is a heart just below a spade.
Name the cards:
Card 1 $\qquad$
Card 2 $\qquad$
Card 3 $\qquad$
7. NAME $\qquad$

Ann found two dollars. She then had five times as much money as she would have had if she lost two dollars.

How much money did Ann have originally?

TODAY'S TWISTER
6. NAME $\qquad$

A boy had two urns; one held exactly three quarts and the other exactly five quarts. His father sent him to the well with instructions to return with exactly four quarts.

The sides of the urns were not marked in any way. How did the boy manage to measure exactly four quarts of water?

Put answer on back.

## TODAY'S TWISTER

8. NAME $\qquad$

Sample: Write three sixes to make six.

Ans. $6 \times 6 / 6$

Write three sixes to make seven.
ANSWER
Write four fours to make five. You may use basic operations, a square root symbol, parentheses, decimal points and exponents (as long as the exponent is a 4).

ANSWER

TODAY'S TWISTER
9. NAME

The number 9 is an intriguing one as you will discover as you fill in the blanks.

$$
(0 \times 9)+1=-
$$

$(1 \times 9)+2=-$
$(12 \times 9)+3=-$
(123 x 9) $+4=--$
$(1234 \times 9)+5=--$
$(12345 \times 9)+6=$
$(123456 \times 9)+7=$
-------
$(1234567 \times 9)+8=$
(12345678 x 9) $+9=$--------
$(123456789 \times 9)+10=-\infty--$
TOTAL= $\qquad$

## TODAY'S TWISTER

10. NAME $\qquad$

Simplify:


Hint: Start at the bottom and work up.

ANSWER $\qquad$
12. NAME $\qquad$

Into how many quarter inch cubes may a one inch cube be cut?
$\qquad$

## TODAY'S TWISTER

13. NAME $\qquad$

What number may be placed in both boxes to make this true?
(Same number in both boxes)


ANSWER $\qquad$

TODAY'S TWISTER
15. NAME

The reciprocal of any number, say $n$, is $1 / n$ (except when $n=0$ ).

By exactly how much does 1.10 exceed its reciprocal?

TODAY'S TWISTER
14. NAME $\qquad$

In a list of four numbers the average of the first two is 15 , the third number is 8 , and the average of the four numbers is $8 \frac{1}{2}$. What is the fourth number?

ANSWER $\qquad$

TODAY'S TWISTER
16. NAME $\qquad$

Move one number from one group to another so that the sum of the numbers in each group will then be equal.
(Answer by using arrows or a description of what to do on back.)

ANSWER $\qquad$
17. NAME $\qquad$

LIST AND ADD all divisors of 220 including 1 but not including 220.
(Note: For your final answer give only the sum of the divisors.)

FINAL ANSWER $\qquad$
18. NAME

Harry and Cary were counting their money. Harry said, "Give me one of your dollars and I'll have as many as you."
"Yes", Cary said. "But if you give me one of your dollars then I'll have twice as many as you have."

Originally, how many dollars did each person have?


## TODAY'S TWISTER

19. NAME $\qquad$

Mr . Barcatchem, carrying his rifle, walks directly south from a point, traveling a distance of three miles. He then walks east for three miles and at that point shoots a bear.

Upon checking his position, he finds that he is still three miles from where he started.

What color is the bear?
TODAY'S TWISTER

TODAY'S TWISTER
22. NAME $\qquad$

Find two numbers whose difference and whose quotient are both equal to three.

ANSWER $\qquad$

TODAY'S TWISTER
24. NAME $\qquad$

Suppose that a pond lily doubles itself every day and at the end of 37 days has half filled a 10,000 acre lake. How many days from the start does it take to fill the lake?

ANSWER $\qquad$

TODAY'S TWISTER
25. NAME $\qquad$

A prime number is divisible by no other number except one. Examples are 5, 7, 19, 41, etc.

Name:
a. The only even prime $\qquad$
b. A prime between 25 and 30
c. A prime between 50 and 55 $\qquad$ $1813+5$ (or $11+7$ )
d. All the primes in the nineties $\qquad$

## 26. NAME

$\qquad$
One mathematician said "Every even number can be expressed as the sum of two primes".
Prove that this is true for each of these even numbers. That is, write the sum of two primes for each even number below. The first one is done as an example.

14 $\qquad$
20 $\qquad$
100


## TODAY'S TWISTER

27. NAME $\qquad$
Below is a "map" of six countries. Only four colors may be used to color the six countries and no bordering countries may have the same color. Which of the pairs of countries listed could possibly have the same color? (Careful - only one answer is possible.)

A \& 0
A
A \&
N \&

$$
\& 0
$$

$$
\mathrm{N}
$$

\& R O \&
\& R
c

ANSWER $\qquad$

## TODAY'S TWISTER

28. 

> NAME
$\qquad$


A plank is pushed forward on rollers as shown. How far does the plank advance if the rollers advance two feet?

ANSWER $\qquad$

## TODAY'S TWISTER

TODAY'S TWISTER
29. NAME $\qquad$ 30. NAME $\qquad$

Below is a set of pins at the end of a bowling alley designed to be struck from the "top". Cross out and rearrange the position of three pins so the group is designed to be struck from the "bottom".

Find the next number in the series.

4, 9, 17, 35, 69,

ANSWER $\qquad$

## TODAY'S TWISTER

31. NAME $\qquad$

Try to guess the rule and use it to finish the last problems.

32. NAME $\qquad$

A cryptarithm is an ordinary arithmetic problem disguised by using letters instead of numbers. You must discover what numbers are being replaced by letters.

What numbers for $L, M$, and $N$ will make this addition example work?

$$
\begin{array}{rl}
\text { L M N } \\
+6 \mathrm{~L} & \mathrm{M} \\
\hline \mathrm{~N} 5 \mathrm{~L} \quad 0 & \text { (zero) }
\end{array}
$$

ANSWER: L = $\qquad$ , $\mathrm{M}=$ $\qquad$ , $N=$ $\qquad$

TODAY'S TWISTER
33. NAME $\qquad$

Among the coins owned by a coin collector was one dated 368 B.C. It was made of gold. Can you tell whether the coin was genuine and if so, how?

TODAY'S TWISTER
34. NAME $\qquad$

Eight persons were in a room. Each person shook hands with each other person. How many handshakes occurred?

## ANSWER:

ANSWER $\qquad$

## TODAY'S TWISTER

35. NAME $\qquad$

Braithenwald walks for three days at the rate of 12 miles per day and for 5 days at the rate of 8 miles per day. What is his average rate of walking in miles per day?

ANSWER $\qquad$
36. NAME $\qquad$

A piece of paper is colored as follows: $1 / 3$ of it is red, $1 / 4$ of it is blue, and the remaining 8 square inches are burgundy.

What was the area of the original piece of paper?

ANSWER

TODAY'S TWISTER
37. NAME $\qquad$

Harry bought a table tennis paddle for $\$ 1.30$ and sold it to Zinger for $\$ 1.30$. Zinger sold it back to Harry for $\$ 1.20$. Next, Harry sold the paddle again for \$1.35. How much did he make on the whole transaction?

ANSWER $\qquad$

TODAY'S TWISTER
38. NAME $\qquad$

How many times does the clock strike during a day if it strikes the correct number of times for each hour?
39. NAME $\qquad$

A man planted ten trees. He had three rows of four trees each.
How did he do it? Draw your answer. had three rows of four trees each.
How did he do it? Draw your answer. had three rows of four trees each.
How did he do it? Draw your answer.

## TODAYS TWISTER

## TODAY'S TWISTER

40. NAME $\qquad$

In a line of girls there were 2 girls in front of a girl, 2 girls behind a girl, and there was a girl in the middle. How many girls were there (minimum number) ?
$\qquad$

TODAY'S TWISTER
41. NAME $\qquad$

There are four tents at a carnival and Betsy enters each one. It costs $\$ 1$ to enter a tent and \$l to exit. Inside each tent Betsy spends half of what is in her pocket. When she emerges from the last tent she has no money left. How much did she have at the beginning?

TODAY'S TWISTER
42. NAME $\qquad$

If 23 (base ?) = 15 (base ten), then what numeration system is the 23 written in ?

ANSWER $\qquad$

ANSWER $\qquad$

TODAY'S TWISTER
43. NAME $\qquad$

Janis determined that it took six seconds for the town hall clock to strike 6. How long will it take this clock to strike 12?

TODAY'S TWISTER
44. NAME $\qquad$

It is now ll:30. When will the hands of the clock next be at right angles with each other?
a. A little before ll:45
b. Exactly quarter of twelve
c. A little after quarter of twelve
d. exactly 12:15
$\qquad$

## TODAY'S TWISTER

45. NAME $\qquad$

If you take this number and triple it, then add 6, and finally double the result, the answer is 57. What is the number?

ANSWER $\qquad$

## TODAY'S TWISTER

47. NAME $\qquad$

GROUND RULE: Same shape must contain the same number.

2 x

$+\square=13$


ANSWER:

$$
\square=
$$

## TODAY'S TWISTER

48. NAME $\qquad$

A woman is 46 years old when her daughter is 18 . How old will the woman be when she is twice her daughter's age?

ANSWER $\qquad$

$$
\begin{aligned}
& \text { TODAY'S TWISTER } \\
& \text { 49. NAME } \\
& \text { If each person in a room shakes } \\
& \text { hands with each other person exactly } \\
& \text { once, how many people are in the } \\
& \text { room if there are } 15 \text { handshakes? }
\end{aligned}
$$

ANSWER $\qquad$

TODAY'S TWISTER
51. NAME $\qquad$

A small purse is full of coins. If you count them by 2's, 3's, or 5's there will be 1 left over. If you count them by 7's there will be none left over. How many coins are in the purse?

TODAY'S TWISTER
50. NAME $\qquad$

If you wrapped a piece of string around the earth exactly once and then made it one foot longer, which of the following would be true?
a. You could barely slip a piece of cardboard under the string.
b. You could just about fit an orange under the string.
c. You could drive a car under the string.

ANSWER $\qquad$

TODAY'S TWISTER
52. NAME $\qquad$

The perimeter of Julie's rectangular garden is 48 feet. What are its length and width if its area is 140 square feet?

ANSWER $\qquad$

TODAY'S TWISTER
53. NAME $\qquad$

Time can be strange. To what does the following refer?

I occur twice in two seconds, once in a fortnight, but not ever in a century. What am I?

ANSWER $\qquad$

TODAY'S TWISTER
55. NAME $\qquad$

Bobby lived on Ronald Road. When asked what the number of his house was he replied, "It has two digits, and when a decimal point is placed between them, the resulting number is the average of the digits in my house number".

What was Bobby's house number?

ANSWER

TODAY'S TWISTER
54. NAME $\qquad$

If three boys can wash three cars in three hours, how long will it take four boys to wash eight cars?

ANSWER $\qquad$
56. NAME $\qquad$

Discover what Rule $\xrightarrow{a}$ is doing to the left number to get the right-hand answer and fill the blanks.


TODAY'S TWISTER
57. NAME $\qquad$

Two bicycle riders are 25 miles apart. One is traveling 15 mile per hour and the other 10 miles per hour. A bee starts from the front tip of the handlebars of one bike and flies to the front tip of the handlebars of the other and then back and forth from tip to tip, always flying at the rate of 20 miles per hour as the bicycles approach each other. How far did the bee fly before the cylists met?

TODAY'S TWISTER
59. NAME $\qquad$

A fence 20 feet long requires four posts. How long would a similar fence be which contains 10 posts?

TODAY'S TWISTER
58. NAME $\qquad$

Suppose that the following statement is true: "If Harry is happy then Sally is sad." What definite conclusion can you draw (if any) if:
a. Harry is happy.
b. Harry is not happy.
c. Sally is sad.
d. Sally is not sad.

ANSWERS :
a. $\qquad$
b. $\qquad$
C. $\qquad$
d. $\qquad$

TODAY'S TWISTER
60. NAME $\qquad$
$\begin{array}{lllllllll}1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9\end{array}$
There are different ways in which the above numbers can be connected to total 99 without changing their order. One solution is:
$1+23+45+6+7+8+9$
Try to find another which, like the example given, uses only addition.

ANSWER $\qquad$

TODAY'S TWISTER
61. NAME $\qquad$

Use the number 3 five times to form the number 31.

ANSWER:
$-$

TODAY'S TWISTER
62. NAME $\qquad$

A circular target with concentric rings has the following numbers printed on it, one in each ring:

16, 17, 23, 24, 36, 40

Tell how exactly 100 could be scored using no more than 6 arrows.

ANSWER:

TODAY'S TWISTER
63. NAME $\qquad$
a. If 13.2 (base $y$ ) $=91 / 3$ (base ten), what number is represented by $y$ ?

ANSWER $\qquad$
b. If 0.13 (base $n)=4 / 27$ (base ten), then $\mathrm{n}=$ $\qquad$

TODAY'S TWISTER
64. NAME $\qquad$

Give the letter of each which is not divisible by 4:
a. $4^{30}$
b. $30^{4}$
c. $4^{35}$
d. $35^{4}$
e. $17^{50}+17^{50}+17^{50}+17^{50}$
f. $17^{50}$ g. $4^{(20-2)}$
h. $4^{20}-2$

ANSWER $\qquad$

## TODAY'S TWISTER

66. NAME $\qquad$
67. NAME $\qquad$

If $4 *=6,9 *=16$, and $50 *=98$,
then $2+(3) *+(2+3) *=? ?$

ANSWER $\qquad$ pass coming from the opposite direction when I go from bus stop A to bus stop B if busses leave each station every ten minutes and the trip takes one hour. Count the bus pulling into $A$ as $I$ leave and leaving $B$ as I arrive.

ANSWER $\qquad$

TODAY'S TWISTER

A bus left Atlanta, Georgia, at 4:00 A.M. and drove toward New York City at 55 miles per hour. At 5:00 A.M. the same day a bus left New York City and drove toward Atlanta at 50 miles per hour. At the instant that the drivers passes each other, which one was closer to New York?.

ANSWER $\qquad$
68. NAME $\qquad$

$A B C$ is a diameter of the large circle with $B$ as its center. Find the area of the shaded S - shaped figure if the area of the large circle is 88 sq. units.
$\qquad$ sq. units

TODAY'S TWISTER
69. NAME $\qquad$

If a driver had increased his speed by one-fourth, he would have made his trip in 16 hours. As it was, how long did it take him to make the trip?

ANSWER $\qquad$

TODAY'S TWISTER
71. NAME $\qquad$

If there are 16 stations on a railroad, how many different tickets are required to connect every station with every other station?

TODAY'S TWISTER
70. NAME $\qquad$

Write 30 using three equal single digits and any basic operation symbols, including exponents.

ANSWER $\qquad$
72. NAME $\qquad$

If a woman buys a half dozen eggs each week for two weeks and then one dozen each week for three weeks, on the average, how many eggs does she use per week?
$\qquad$
73. TODAY'S TWISTER

NAME $\qquad$

Three men at 6:00 A.M. started to dig two holes. One of them, workalone, completed his hole, $3 \times 3 \times 3$, in one hour. The other two, each working at the same speed as the first, made their hole $6 \times 6 \times 6$. How long did it take them?

ANSWER $\qquad$

TODAY'S TWISTER
74. NAME $\qquad$

Remembering that:
Odd no. + even no. = odd no. Odd no. + odd no. = even no. Even no. + even no. = even no.

What are the chances, given a pair of identical twelve sided dice with any consecutive 12 numbers printed on their faces, that a total which is an even number will be rolled?

ANSWER $\qquad$

TODAY'S TWISTER
76. NAME

Use four 7's to express the number 87.

$$
\begin{gathered}
\text { Sample: } 77 / 7-7=4 \\
\text { (not right for } 87 \text { ) }
\end{gathered}
$$

Decimal points and parentheses may also be used.

ANSWER $\qquad$ 54 ft . and width 12 ft . is to have posts put around it 3 feet away from the garden's edge on all sides. They are also to be three feet apart. How many posts will she need?
77. NAME $\qquad$ 78. NAME $\qquad$

Eleventeen and $2 / 3$ of eleventeen is what part of $7 / 3$ of eleventeen?

ANSWER $\qquad$

## TODAY'S TWISTER

79. NAME $\qquad$

Janis says that three men can build a garage in 4 days, and if it takes ten boys to do the work of four men, how long will it take two men and three boys to build the garage?

## TODAY'S TWISTER

80. NAME $\qquad$

Roger noted that there is a cube which has the same number of square units in its surface area as it has cubic units in its volume. How many units in the length of the edge of the cube?

ANSWER $\qquad$

ANSWER $\qquad$

## TODAY'S TWISTER

81. NAME $\qquad$

Leslie got up early one morning to deliver newspapers. It was still dark outside and none of the lights in the room would work. Leslie knew that there were 10 red socks and 4 white socks in the dresser drawer. What is the minimum number of socks that leslie has to pull out of the drawer in the dark to be sure that there are at least two that match?

TODAY'S TWISTER
82. NAME $\qquad$

If a goose and a half can lay an egg and a half in a day and a half, how many eggs can seven geese lay in six days?

ANSWER $\qquad$
ANSWER $\qquad$

TODAY'S TWISTER
84. NAME $\qquad$

Let $n$ mean $2 x n-3$ and let $n$ mean $n^{2}+1$.

What value of $Y$ will make the following true?


ANSWER $\qquad$

## TODAY'S TWISTER

## TODAY'S TWISTER

85. NAME $\qquad$

Two cowboys were complaining about their horses, each insisting that his own horse was slower than his partner's. To settle the matter they agreed to a race in which the horse to cross the finish line last would be declared the winner, having proved to be the slower.

They started to race across the Arizona desert but soon slowed to a complete stop, each rider being reluctant to prove himself wrong. They dismounted and explained their dilemma to a passing man who made a suggestion, whereupon the men immediately mounted and raced for the finish line. What was the suggestion?

ANSWER $\qquad$

TODAY'S TWISTER
87. NAME $\qquad$

In the bottom of a well 33 feet deep there was a frog who began to travel toward the top. In his journey he ascended three feet each day and slipped back two feet each night. In how many days did he get out of the well?

ANSUTER $\qquad$
List each number which will make this sentence true (same number in all boxes at one time).


ANSWER $\qquad$ <br> TODAY'S TWISTER <br> \section*{TODAY'S TWISTER} <br> \section*{TODAY'S TWISTER}
88. NAME $\qquad$

How can this board be cut into two pieces so it will exactly cover the hole? Draw the cut line and lable its dimensions.

89. NAME

Let $n$ mean $(n+2)^{2}$,
Let $n$ mean $n^{2}+2$, and
Let $n$ mean $n-5$.
Enclose (-l) within three shapes, not necessarily different shapes, so as to produce the largest possible result and tell what that result is. Example (not the right one!):


Hint: It's possible to produce a value much larger than 500.
90. NAME $\qquad$

What number is just as much less than 92 as its triple is more than 92?

ANSWER $\qquad$

## TODAY'S TWISTER

92. NAME $\qquad$
Tom, Dick and Harry were on a camping trip. Tom brought out a bag of cherries for an evening snack just as the other boys were falling asleep. Tom ate his share and fell asleep. Later, Dick woke up, ate what he thought to be his share and fell asleep. Then Harry awoke, ate whate he thought to be his share, and fell asleep. Morning came and there were eight cherries left. After some discussion, the boys were able to determine how many of the eight cherries each person should get so that each received a third of the original number. How many did each get?

ANSWER: TOM $\qquad$ DICK $\qquad$ HARRY $\qquad$

TODAY'S TWISTER
93. NAME $\qquad$

How many inches in the circumference of a circle whose area is 154 square inches?

Use pi $=22 / 7$

ANSWER $\qquad$

TODAY'S TWISTER
95. NAME $\qquad$

Braithenwald deposited $\$ 1$ in January, $\$ 2$ in February, $\$ 4$ in March, \$8 in April, etc.
a. How much money will he have after his December deposit?
b. If he continues, what will be the amount of the l3th deposit in January of the second year?
c. How much money will he then have? ANSIVERS a $\qquad$ b. $\qquad$ C. $\qquad$
96. NAME $\qquad$

Two freight trains are traveling in opposite directions, one east at 45 miles per hour and the other west at 60 miles per hour. A man on the eastbound train is running west along the tops of the cars at the rate of 10 miles per hour and a man on the westbound train is running west at the rate of 15 miles per hour. At what rate do the two men pass each other when the trains pass?
$\qquad$

## TODAY'S TWISTER

97. NAME $\qquad$

$Q$ is the center of the large circle and $P$ is the center of the small circle. How far does point $P$ travel while the small circle runs once around the inside of the large one if the circumference of the large circle is 22 inches?

ANSWER $\qquad$

## TODAY'S TWISTER

99. NAME $\qquad$

Which one of the following list of inequalities should be left out so that so that none of the remaining four will contain contradictions?
$\mathrm{a}>\mathrm{b}$
$a>d$
$\mathrm{b}>\mathrm{c}$
$\mathrm{c}>\mathrm{a}$
$\mathrm{d}>\mathrm{c}$

## TODAY'S TWISTER

98. NAME $\qquad$

Here is a three inch cube which has been painted red. It is then cut into one inch cubes along the lines indicated. How many of the resulting one inch cubes have exactly:
a. 6 painted surfaces ?
b. 5 painted surfaces ?
c. 4 painted surfaces ?
d. 3 painted surfaces ?
e. 2 painted surfaces ?
f. 1 painted surface ?
g. 0 painted surfaces ?


## TODAY'S TWISTER

100. NAME $\qquad$

Evaluate this continued fraction:

$$
2+\frac{2}{2+\frac{2}{2+\frac{2}{2+\frac{2}{2+\frac{2}{2+2}}}} 1}
$$

ANSTIER $\qquad$

ANSWER $\qquad$

## TODAY'S TWISTER

101. NAME $\qquad$
$\sqrt{25}=5, \quad \sqrt{36}=6 \quad \sqrt{100}=10$
$4!=4 \times 3 \times 2 \times 1, \quad 9!=9 \times 8 \times . \quad . \quad . \times 3 \times 2 \times 1$ (Remember factorials?)

Simplify:
$\left(\begin{array}{llllll}4 & \times \sqrt{\frac{36}{100!}} \times 99! & \times & \frac{5}{3}\end{array}\right)!$

ANSWER $\qquad$

## TODAY'S TWISTER

103. NAME $\qquad$

A field is owned by three people. A has three-fifths of it and $B$ has twice as much as $C$. What fraction of the field belongs to C?

## TODAY'S TWISTER

104. NAME $\qquad$

The Big Indian and the Little One

A big Indian and a little Indian were sitting on a fence. The little Indian was the big Indian's son but the big Indian was not the little Indian's father. How could this be?
$\qquad$

```
TODAY'S TWISTER
```

105. NAME

Suppose the pond ponger reproduces by dividing in two every day. On the first day there is one, on the second day 2 , the third day 4 , etc. If, starting with one pond ponger, it takes 20 days to cover a certain area, how long will it take to cover the same area starting with two pongers?

ANSWER $\qquad$
107. NAME $\qquad$

Let $8_{4}$ mean $8+9+10+11$ ( 4 terms), and 53 mean $5+6+7$ ( 3 terms).

Evaluate:

$$
21,408_{5}-21,406_{5}
$$

ANSWER $\qquad$
106. NAME $\qquad$

As the number in the box gets larger and larger, what value does the complex fraction approach?


ANSWER $\qquad$

TODAY'S TWISTER
108. NAME $\qquad$


Set A contains all the two digit whole numbers.
Set $B$ contains all the primes.
Set $C$ contains all whole numbers whose final digit is 1.

List the numbers which belong to the shaded area.

ANSWER $\qquad$

TODAY'S TWISTER
109. NAME $\qquad$

If four boys can wash four
cars in six hours, how long will it take three boys to wash six cars?

ANSWER $\qquad$
110. NAME $\qquad$

If Mary weighs $112 \frac{1}{2}$ lbs. and Ann weighs 100 lbs., for every 18 lbs. that Mary weighs, there are how many pounds in Ann's weight?

TODAY'S TWISTER

ANSWER $\qquad$
111. NAME $\qquad$
Sue wrote the sum of the numbers from 1 to 100 and underneath, wrote the sum backwards.

| 1 | + | + | $+98+99+100$ |
| :--- | ---: | ---: | ---: |
| $100+99$ | + | + | $+3+2+$ |

From this she was able to find a short cut for adding up all the whole numbers from 1 to l00. See if you can do it.
112. NAME $\qquad$

Braithenwald spent $1 / 3$ of his money for candy, $1 / 4$ of his money for soda, and $1 / 5$ of his money for ice cream. If he then had 26 ¢ left, how much did he have at the start?

ANSWER $\qquad$

ANSWER $\qquad$
113. NAME

Boxes of cookies are arranged as shown below in a square pattern. Stacks of seven alternate with single boxes. A clerk in the store sold four boxes and then rearranged the stacking, keeping the square pattern and also keeping nine boxes on each side of the square. Show how he did it.
$\begin{array}{lll}1 & 7 & 1\end{array}$
$\begin{array}{ll}7 & 7\end{array}$
$\begin{array}{lll}1 & 7 & 1\end{array}$
114. NAME $\qquad$

Subtract four thousand fourteen hundred and one-half from thirteen thousand thirteen hundred thirteen and one-half.

ANSWER $\qquad$
115. NAME $\qquad$

If a match and a half costs a penny and a half, how much will 11 matches cost?

ANSWER $\qquad$

TODAY'S TWISTER
116. NAME $\qquad$

If $I$ add 1000 to a certain whole number, the result is more than if I had multiplied that number by 1000. What is the number?

ANSWER $\qquad$

TODAY'S TWISTER
117. NAME $\qquad$

Name all the positive or negative whole numbers which, when multiplied by themselves, are equal to two more than themselves.

ANSWERS $\qquad$
119. NAME $\qquad$

A boy bought a bat and a ball for $\$ 1.25$. If the bat cost 25 个 more than the ball, how much did each cost?
118. NAME $\qquad$
Make a Magic Square by putting in the numbers l - 9 so that the sum of the horizontals, the verticals and the diagonals equals 15.


## TODAY'S TWISTER

120. NAME $\qquad$

If it takes seven seconds for a clock to strike seven, how many seconds does it take to strike ten?

ANSWER $\qquad$

TODAY'S TWISTER
121. NAME $\qquad$

This one takes patience. There is a solution which involves only addition (no exponents, square root, subtraction, etc.).

Use eight 8's to make 1000 .

ANSWER $\qquad$

TODAY'S TWISTER
123. NAME $\qquad$

A farmer was asked whether he had a score of pigs. He said that he did not but if he had as many more, and half that many more, plus two pigs and a half, he would then have a score.

How many pigs did he have?

## TODAY'S TWISTER

122. NAME

Let $(8,11)$ mean the interval of all numbers from 8 to 11 but including neither the 8 nor the 11 . Some members are $81 / 3,9.3067$, $101 / 2$, $10 . \overline{89}$, etc.

How many multiples of 6 are members of the interval:
$(200022,200844) ?$
Use some ingenuity; don't just count!

ANSWER $\qquad$

TODAY'S TWISTER
124. NAME $\qquad$

How many degrees are there between the hands of the clock at 4:40?

ANSWER $\qquad$

TODAY'S TWISTER
125. NAME $\qquad$

By how much does the sum of the reciprocals of $2 / 5$ and 2 exceed the reciprocal of their sum?

ANSIVER $\qquad$

## TODAY'S TWISTER

127. NAME

Suppose we know for certain that:
If Gretchen is grateful, then Hortence is hopeful.

Then which, if any, of the following statements are true?

1. If Gretchen is not grateful, Hortence is not hopeful.
2. If Hortence is hopeful, Gretchen is grateful.
3. If Hortence is not hopeful, Gretchen is not grateful.

ANSWER $\qquad$

TODAY'S TWISTER
126. NAME

Without computing, name all
the whole numbers less than eleven
by which you know that
$(2 \times 3 \times 4 \times 5 \times 6 \times 7 \times 8 \times 9+1)$
is not divisible (evenly).

ANSWER $\qquad$
128. NAME $\qquad$

One window is one-half a yard square. Another window has an area of one-half square yard. The area of the first window is what fractional part of the second?

ANSWER $\qquad$

## TODAY'S TWISTER

129. NAME $\qquad$


Count the triangles in this figure. Get all of them!

ANSWER $\qquad$
130. NAME

## TODAY'S TWISTER



The left hand log has a knot on the end and near the top. That $\log$ is rolled over the log in the middle to the position at the right. Show the location of the knot in the right hand position.

## TODAY'S TWISTER

131. NAME $\qquad$
$\left[\begin{array}{ll}5 & 2 / 3\end{array}\right]=5,[3.2]=3$. That is,
$[n]$ means to take only the greatest
integer in $n$. Thus, $\left[\begin{array}{ll}2 & 1 / 2\end{array}\right]=2$, $[100]=100,[0.3]=0$.

Do these:
a. $[2141 / 151]+[699 / 110]$
b. $[2141 / 151+699 / 110]$
c. $\left[250 / 101+3 \begin{array}{l}51 / 100 \\ \text { don't }\end{array}\right] \begin{gathered}\text { (Think, }\end{gathered}$

ANSWERS: a $\qquad$ b. $\qquad$ C. $\qquad$

## TODAY'S TWISTER

## 132. NAME

$\qquad$

There are three volumes of books, identical in size and shape, standing next to one another in order. , A bookworm begins at the first page of Volume $I$ and eats his way through to the last page of Volume III. If each book is 2 3/4 inches thick with the pages representing $21 / 2$ inches of this, how far does the bookworm travel?

ANSWER $\qquad$
133. NAME $\qquad$

A man had $\$ 1.15$ in coins, all less than a dollar, in his pocket. Still, he could not make change for a dollar, a half dollar, a quarter, a dime or a nickel. What coins did he have in his pocket?
134. NAME $\qquad$

Mrs. "M" said,
"I have no sister and I have no brother, but that girl's mother is daughter to my mother."

Who is "that girl"?

ANSWER $\qquad$

## TODAY'S TWISTER

136. NAME $\qquad$

Four 4's can be used to express numbers such as:
$2=4 / 4+4 / 4,3=\sqrt{4+(4 \div 4)+4}$
$4=\sqrt{4}+\sqrt{4}+4-4$

Use four 4's to express 11. Any of the above symbols may be used as well as multiplication and decimal points.

ANSWER $\qquad$
List the letter of each number which is not the square of some integer:
a. 2501 b. 81 c. $\sqrt{81}$
d. 25.25 e. $90,000,000,000,000$
f. $16,000,000$ g. 30,147
h. $39 \times 3 \times 13$ i. $6^{15}$
j. -100

ANSWER $\qquad$

## TODAY'S TWISTER

137. NAME

When Penelope broke her bank and counted all her pennies she found that when she counted them two at a time there was one left over. Also, when she counted them three, four, five or six at a time, there was always just one left over. What is the smallest number of pennies that Penelope could have had in her bank if, when she counted them seven at a time, there were none left over?

TODAY'S TWISTER
138. NAME $\qquad$

Show using a drawing how six toothpicks may be glued together to form four equilateral triangles which are congruent (same size and shape).

## TODAY'S TWISTER

139. NAME $\qquad$
Recall that $[\mathrm{n}]$ means the largest whole number in $\mathrm{n}:[8.7]=8,[5 / 8]=0$
etc. What is the smallest whole number which can be put in both boxes so this sentence will not work?


TODAY'S TWISTER
140. NAME $\qquad$

How long would it take to cut a 387 inch length of string into 9 inch lengths if each cut takes two seconds?. Only one string is cut at a time.
$\qquad$
141. NAME $\qquad$

Two cyclists start at the same time from the same place and travel to a common finish point at the other side of a hill. Tom travels over the hill, averaging 3 miles per hour up for the first half and 11 miles per hour down for his second half. Sue goes around the hill at a constant 7 miles per hour. Which of these is correct if their total distances are equal?
a. Tom beats Sue
b. Sue beats Tom
c. They tie
d. Not enough information to tell

ANSWER $\qquad$

ANSWER $\qquad$
144. NAME $\qquad$

## TODAY'S TWISTER

Which of the following is (are) evenly divisible by $2,3,6$ and 9 (by all four numbers)?

| 156 | 236 | 5,364 |
| :---: | :---: | ---: |
| 4,010 | 1,010 | 207 |

143. NAME $\qquad$ (by all four numbers)?

4,010
1,010
207

True of false:
The statement "4/.03 is not
greater than $3 / .03$ " is not false.
True of false:
The statement "4/.03 is not
greater than $3 / .03$ " is not false.
True of false:
The statement "4/.03 is not
greater than $3 / .03$ " is not false.

ANSWER $\qquad$

## 142. NAME

$\qquad$

Name five numbers less than 20 which, when squared, give perfect cubes. Each number contains only one digit.

ANSWER $\qquad$


## TODAY'S TWISTER

TODAY'S TWISTER
145. NAME

Four boys have three pizzas to share. The pizzas have diameters of nine, twelve, and fifteen inches. Can you describe a way to divide the pizzas fairly using only 3 cuts?

ANSWER:
146. NAME

A girl went to a booth in an amusement park and said to the proprietor, "If you give me as much money as I now have then I will spend $\$ 10.00$ at your booth. It was done and repeated at a second and third booth. How much money did the girl have when she started at the first booth if she finished with no money left?

ANSWER $\qquad$
147.

TODAY'S TWISTER

NAME $\qquad$

Back when $\$ 2$ bills were in circulation a man bought a watch for \$103 including tax. Being rather an unusual person he paid for it in eight bills. How could this have been done if:
a) He used any bills except $\$ 2$ bills
b) He used any bills except $\$ 1$ bills

ANSWERS: a)
b) $\qquad$

TODAY'S TWISTER
148. NAME $\qquad$

A conversation heard on a bus:
Man: "Was he related to you?"
Woman: "Yes. That gentleman's mother was my mother's mother-in-law, but he was not on speaking terms with my father."

Man: "Of course." But you could see that he was not a lot wiser.

How was the gentleman who was referred to by the woman related to the woman?

ANSWER $\qquad$

## TODAY'S TWISTER

149. NAME $\qquad$

$$
\sqrt{\square}=2 \times \square
$$

Name all the numbers which will make the above sentence true. (Same number in both boxes at once.)

ANSWER $\qquad$

TODAY'S TWISTER
150. NAME $\qquad$

Nicotine Nelly walked along the street picking up cigarette butts and used the tobacco in them to roll her own. If a standard size cigarette can be rolled out of six standard size butts, how many cigarettes can be rolled and smoked if Nellie finds 36 standard size butts?

ANSWER $\qquad$

> TODAY'S TWISTER
152. NAME $\qquad$

If a number appears in a triangle, it means to double the number and add 3.
Thus, $4=11$
And suppose that (n) means to find the reciprocal of the number.

Find the value of:
a) $4+4=$
b)


TODAY'S TWISTER
153. NAME $\qquad$

A certain prime number between 100 and 200 is the same when written backwards but when written upside down and looked at in the mirror, is divisible by 7. What is it?

ANSWER $\square$
155. NAME $\qquad$

Twice a fraction plus half that fraction times that fraction equals that fraction. What's the fraction?

TODAY'S TWISTER
154. NAME $\qquad$

Mr. Tazzlewourtz hired a boy at a certain hourly wage; reduced his wage by ten percent, and later raised it by ten percent. The boy's new wage was then $2 \dot{c}$ less than the old. What was the new hourly wage?

ANSWER $\qquad$

TODAY'S TWISTER
156. NAME $\qquad$

A is less than B. If $C$ is less than $B$ then $D$ is greater than $E$. What single definite conclusion can you come to regarding $A$ if $D=5$ and $E=6$ ?

ANSWER $\qquad$

## TODAY'S TWISTER

157. NAME

On a chessboard of 64 squares a man agreed to put a penny for his son on the first square the first day, 2 ( on the second square the second day, $4 \dot{\xi}$ on the third square the third day, then 8 ¢, 16\%, etc. How much money would he have given his son after 64 days?
a. About $\$ 100$
b. About $\$ 60,000$
c. About 90 million dollars
d. About 18 quintrillion dollars
158. NAME $\qquad$

There are less than six dozen eggs in a basket. If I count them two at a time, there is one left. If I count them three at a time there are two left. If I count them four at a time there are three left. And if $I$ count them five at a time there are four left. How many eggs are there in the basket.

ANSWER $\qquad$
ANSWER $\qquad$

## TODAY'S TWISTER

159. NAME

$$
1 / 2+1 / 5+1 / 7=47 / 70
$$

Find a set of fractions having different denominators but all having numerators of 1 so that the fractions add up to 17/31.

Hint: $1 / 2=15 \frac{1}{2} / 31$

ANSWER $\qquad$

## TODAY'S TWISTER

160. NAME

Between ten and twenty there are two consecutive integers which, when squared, have the same digits in different order. What are they?

ANSWER $\qquad$

TODAY'S TWISTER
161. NAME $\qquad$

Two mothers and two daughters left town. This resulted in a reduction in the population of three. How could this be?

ANSWER: $\qquad$
163. TODAY'S TWISTER

NAME $\qquad$

Compute in simplest form the reciprocal of the sum of the reciprocals of 0.5 and 3 .

ANSWER $\qquad$
162. NAME $\qquad$

Halenthorpe rides his bike 5 miles to his grandmother's house at the rate of 10 miles per hour.

At what rate should he return home so that the average rate for the whole trip will be 12 miles per hour?

ANSTWER $\qquad$
164. TODAY'S TWISTER

NAME $\qquad$
(Dirty trick problem)

Give the next three terms of
this series:

$$
\mathrm{O}, \mathrm{~T}, \mathrm{~T}, \mathrm{~F}, \ldots{ }^{\prime} \quad{ }^{\prime}
$$

165. NAME $\qquad$ 166. NAME $\qquad$
If a question is not fair, say so. If it is fair, give the answer.
Recall that $[n]$ means the largest integer in n .
a. $\left[(0.9)^{100}\right]=$ $\qquad$
b. $[0.9]^{100}=$ $\qquad$
c. $\left[(1.9)^{100}\right]=$ $\qquad$
d. $[1.9]^{100}=$ $\qquad$
Evaluate:


ANSWER $\qquad$

TODAY'S TWISTER
167. NAME $\qquad$

How many degrees are there between the hands of the clock at 12:01?

A can do a piece of work in 7 days. $B$ is $50 \%$ more efficient than A. How many days will it take $\underline{B}$ to do the same piece of work?
$\qquad$

## TODAY'S TWISTER

169. NAME $\qquad$

As the denominator of a fraction increases, the value of the fraction decreases:

$$
1 / 2,1 / 3,1 / 4, \text { etc. }
$$

What value does this complex fraction get closer and closer to as the number represented by $y$ increases?
$\frac{1}{1-\frac{1}{\bar{y}}}$

## TODAY'S TWISTER

170. NAME $\qquad$

What perfect square numbers having two digits give prime numbers when decreased by two? Name all of them.

ANSWERS $\qquad$
171. NAME $\qquad$

Three quickies; get them all.

1. Four years ago the sum of the ages of two children was 11 years. What is their sum now?
2. Bill can wax a car in 3 hours and Tom can wax it in 6. Working together they can wax it in hours.
(The answer is one of these: 2 hours, $4 \frac{1}{2}$ hours, 9 hours.)
3. Atty Timwater had seventeen white mice and all but five died. How many did he have left?

TODAY'S TWISTER
172. NAME

Two math classes took the same test. One class of twenty students had an average grade of $80 \%$. The other class of 30 students had an average grade of $70 \%$. What was the average grade of all students in both classes?

ANSWER $\qquad$
173. NAME

A man was buying a certain item at the store. The clerk said:
"One costs ten cents. Seven will cost ten cents. Eleven will cost 20¢."

What was the man buying?

AinSwer $\qquad$

TODAY'S TWISTER
175. NAME $\qquad$

Today Billy is half as old
as his mother. Twelve years ago, Billy was $1 / 3$ as old as his mother was then. How old is each today?

ANSWERS:
Mother $\qquad$
Billy $\qquad$

## 174.

NAME $\qquad$

On the number line a (+6) tadhopper starts on 1 and jumps forward to 7, 13, 19, etc. Also, a. (-4) tadhopper starts on 109, hops downward to $105,101,97$, etc. Name all the numbers they both touch in common (not necessarily at the same time) between 45 and 89.

ANSWER $\qquad$
176. NAME

AAAA $A A A B$ AABA AABB ABAA ABAB ABBA ABBB

TODAY'S TWISTER
$\qquad$ $\longleftarrow$ ANSWERS

## TODAY'S TWISTER

177. NAME $\qquad$

Six points are spaced equally around a circle. How many different straight lines can you draw so that each connects two of the points?


ANSWER $\qquad$

TODAY'S TWISTER
180. NAME $\qquad$
list the letter of each which always has an even number as an answer.
a. The sum of three consecutive whole numbers
b. The product of three consecutive whole numbers
c. The sum of four consecutive whole numbers
d. The sum of five consecutive whole numbers

ANSWERS $\qquad$

## Twister Answers 1 and Some Solution Comments.

7

1. 314 or any of its $\quad 2.24 \quad 3.91 \& 130$ 586 rotations 2
2. Move the right horizontals to the centers of the rectangles. This makes three overlapping rectangles.
3. Jack of spades, queen of spades, queen of hearts.
4. Fill 5 , dump into 3 , empty that 3 . Dump the remaining 2 room the 5 into the 3 . Fill the 5 , dump into 3 's space (1). 4 are now left in the 5 ! You can also start with $3 \&$ get 5 .
5. $\$ 38$ a. $6+6 / 6$ b. $\sqrt{4}+\sqrt{4}+4 / 4$. Other solutions possible. 9.123455678900 ; curve ball question: ones should be added diagonally to stay in proper place value columns. 10987654321 is not correct.
6. $107 / 12 \quad 11.28 \quad 12.64 \quad 13.30 \quad 14 .-4 \quad 15.21 / 110 \quad 16$. Move the nine from the last group to the first. 17. 284. Divisors are $1,2,4,5,10,11,20,22,44,55$ and 110.
7. Harry $\$ 5$, Cary $\$ 7$ 19. White. This happens only with the North Pole as a starting point. Geometrically, it could also start 3+ miles from the South Pole but there are no bears there.
8. 80 cents. 21. Build it on the North Pole. 22. $4 \frac{1}{2}$ and $1 \frac{1 / 2.2}{}$ 23. 345676543 (no perfect square can end in 3. 24.38 days. 25 a. 2 b. 29 c. 53 d. 97 26. Many possible answers. 27. O and R ( $\operatorname{not} \mathrm{N}$ and O ) 28.4 feet
30 . Double and add 1 , double and subtract one, etc.
9. $124,86,11,9,3(\operatorname{not} 6), 5.32 . a=8, b=9, c=1$
10. Not genuine. The coin minter could not have know about "before Christ" before Christ.
11. $2835.9 \frac{1}{2}$ (miles per day). 36 . $191 / 5$ sq. in. 37 . 15 cents. 38. 156
12.     * $\quad * * * 40.3$ 41. $\$ 45$ 42. Base six $43.131 / 5$ seconds ${ }^{* * * *}$ or ${ }_{*}^{*} \quad(11 / 5$ seconds per interval)

* ****

44. a

45. $\square=3, \square=748.5649 .6$ (Note: This is the inverse idea of \#34)
46. $\square=3, \square=748.5649 .6$ (Note: This is the inverse idea of \#34)
47. b. This would work for the moon or a basketball, and it could be verified for them.
51.91 52. 14, 10 53. The letter "o" 54.6 hrs. 55. 45 56. -2, 97, 8, 4, (Square and
48. 20 miles. (It takes the cyclists one hour to meet) subtract 1.)
49. a. Sally is sad b. No conclusion c. No conclusion d. Harry is not happy

## Twister Answers 2 and Some Solution Comments.

59.60 ft . ( $62 / 3 \mathrm{ft}$. per interval) $60.12+3+4+56+7+8+9$
61. $33-3+3 / 3,3^{3}+3+3 / 3$, others possible 62 . $4-17$ 's \& $2-16$ 's 63 a. 6 b. 9
64. d, f, h 65. 14 66.13-It is easy to forget those busses enroute as he leaves plus those that depart while he is enroute.
67. Neither - both distances equal.
68. 22 ( $1 / 4$ of the area of the large circle, since the small semicircles' radii are $1 / 2$ the larger.
69. 20 hours. A $1 / 4$ increase gives a $5 / 4$ speed ratio. Time ratio is inverse, or $4: 5$, hence 20 hours.
$70.3^{3}+3 \quad 71.120 \quad 72.4 / 5$ doz., 9.6 eggs $\quad 73.4$ hours $\quad 74.1 / 2$ or $50-50$. Even + odd reminder not in problem. 75.26 76. $77+7 / 7$ (others?) 77. 5/7
78. All true, though many won't agree, (e) follows from (a-d). 79. $3 \frac{3}{4}$ days. One boy is equivalent to $2 / 5$ man so, " $31 / 5$ men" are working, needing $3 /(31 / 5)$ of 4 hours.
80.6 units $\quad 81.3 \quad 82.2811$ goose lays 1 egg in $1 \frac{1}{2}$ days; in 6 days ( 4 times as long), $4 \times 7=28$ eggs laid.
84. 9/58 85. Exchange horses
86. No number; 2 results in

or a rotation of this
87. 31 days
 division by 0 .

90. 46 91a. 40,320 b. 9,506 92. Tom-0, Rick-3, Harry-5 93. 44 (inches)

94 a. 64 b. $512 \quad 95$ a. $\$ 4095$ b. $\$ 4096$ c. $\$ 8191 \quad 96.110 \mathrm{mph} \quad 97.11 \mathrm{in}$.
98a. 0 b. 0 c. 0 d. . 8 e. . 12 f. . 6 g. . $1 \quad$ 99. c >a $100.219 / 26 \quad 101.24$
102. 18 103. $2 / 15$ 104. The big Indian was his mother. 105. 19 days 106. 3
107. 10 108. 11, $31,41,61,71$ 109. 12 hours: 1 boy -1 car in 6 hours, so 3 boys in 6 hours; 12 hours needed.
110. 16 lbs . 111. 5,050 Add the rows; there are 100101 's, twice the sum (two rows); 252
112. $\$ 1.20$ 113. $\quad 5 \quad 5 \quad$ 114. 9813 . Note: four thousand fourteen hundred $=$ 252

$$
\begin{equation*}
4000+1400=5400 . \tag{816}
\end{equation*}
$$

116. . 1 or 0 117. $-1,2$ 118. 357 or one of its rotations. 119. 50 cents \& 75 cents. 492
117. $10 \frac{1}{2}$ seconds; $11 / 6 \mathrm{sec}$. per interval between strikes, 9 intervals, 9 times $11 / 6=$

$$
101 / 2
$$

121. $888+88+8+8+8$. (Other solutions?) 122. $136 ; 822 / 6=137 ; 136$ 'separators'
122. 7 124. 100 degrees; the hour hand moved $2 / 3$ of the 30 degrees between $4 \& 5$.

## Twister Answers 3/3 and some solution comments.

125.2 7/12 126. 2 through 10. "The product" can share no factors with "the product plus 1 " (no two consecutive numbers can have factors in common except thee factor 1. 11 is the first possibility.
127. \#3. \#1 and \#2 are often implicit in speech but do not follow logically.
128. $1 / 2(21 / 4 \mathrm{sq}$. ft. to $41 / 2$ sq. ft.) 129. 35. There are 7 kinds of triangles, 5 of each.
130.

- 131a. 8 b. 9 c. 6 . Note the difficult reasoning needed in part c.
$51 / 100$ exceeds $1 / 2$ by more than $50 / 101$ falls short of $1 / 2$.

132. 3" 133. Half dollar, a quarter, and 4 dimes. 134. Mrs. M's daughter.
133. $11=4 / .4+4 / 4$; others (?) . 136. a, $d, e, g, i, j$. e has odd number of zeros.
g ends in 7. i has odd number of 6 's multiplied. ( 10000 is a square of an integer, 1000 is not.)
134. 301 138. A tetrahedron 139. 3 140. 84 seconds
135. b ; there is a weighted average here. Tom spends more time at his slower rate.
136. $-8,-1,0,1,8 . \quad$ 143. 5364 (Use divisibility rules.)
137. False 145. The sum of the two smallest pie areas equals the largest so cut each in half. 1 big half = a medium half plus a small half. Note: this could be done with 1 cut if pies are stacked concentrically.
138. $\$ 8.75$ 147. a. $50,20,20,5,5,1,1,1$ b. $50,20,20,5,2,2,2,2$.
139. Her uncle 149. 0 and $1 / 4$ 150. 7 - Don't forget the cigarette accumulated from the butts her smoking creates!
140. 11:48 A.M., a toughie. The time ratio is $2: 3$ ( 5 parts). The fast train goes $3 / 5$ of its total time while the slower train goes $2 / 5$ of its total time. Either way, $3 / 5 \times 8=2 / 5 \times 12=44 / 5$ hours (after 7 A.M.).

152a. $11 \frac{1}{1} 4$ b. 29/33 $153.191154 . \$ 1.98 \quad 155.2 / 5 \quad 156 . a<b$
157. d. 158. 59 159. $1 / 2+1 / 31+1 / 62 \quad$ 160. 13 and 14 161. Grandmother, mother and daughter.
162. 15 mph (Hard!) 10 (dist.) $/ 12=5 / 6 \mathrm{hr} .1 / 2$ hour to go, so $1 / 3 \mathrm{hr}$. to return. 5 (return distance) $/(1 / 3)=15$
163. 3/7 164. F,S,S - first letters of Five, Six, Seven.
165. a. 0 b. 0 c. not fair d. 1 166. 20,000 : common error: $\sqrt{10^{16}}=10^{4}$
167. $51 / 2$ degrees The minute hand goes 6 degrees of clock face arc and the hour hand goes $1 / 12$ as far, or $1 / 2$ degree. $6-1 / 2=51 / 2$.
168. $42 / 3$ days $50 \%$ more means $3 / 2$ times, taking $2 / 3$ of A's time. 169. 1
170. $25,49,81 \quad$ 171. 19, $2,5 \quad 172.74 \% \quad 173$. House numerals $174.49,61,73,85$.
175. 48,74 176. BAAA, BAAB 177. 15 178. a, b, d 179. 32,16 180. b, c

